

Research on Authorization Verification Methods for Message Signatures Within Multi-Level Groups

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Abstract. With the widespread adoption of digital signature, a variety of specialized digital signature methods have been developed. However, the need for authorization verification within hierarchical group structures has not garnered sufficient attention. This research has addressed this issue. Initially, the problem was delineated and formally articulated; subsequently, encryption and decryption algorithms that incorporate authorization sharing were designed, along with a description of the code; finally, the methods were validated through experimentation. The outcomes demonstrate that the proposed approach is reliable and stable, capable of effectively accommodating the authorization verification of signed messages within multi-tiered, large-scale group communications. This addresses the shortfall of current digital signature technologies, which struggle to authorize multiple verifiers within hierarchical group structures, by supplementing and refining a method for the authorization verification of signed messages among users in multi-level groups.

Keywords. Digital signature, hierarchical groups, encryption, decryption, authorization verification

1. Introduction

Whether it is government agencies, public institutions, enterprises, or social organizations, their internal organizations are hierarchical and divided by job responsibilities. The messages transmitted within the organization are also divided by topics. Generally, the messages transmitted within the organization need to be authorized to different levels or members with different responsibilities according to the different topics they belong to. The authorized person may be one or multiple. This is a very common application scenario. However, the existing digital signature technology mainly focuses on improving the security, anonymity, and untraceability of message transmission, but the demand for authorization verification within multi-level groups has not received enough attention.

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2. Related Work

2.1. Traditional digital signature technology

Diffie and Hellman first introduced the concept of electronic signatures in 1976, and in 2003, Anderson R. provided a comprehensive definition of digital signatures.[1] It is based on the public/private key cryptographic system and is essentially an application of asymmetric encryption technology.

Common digital signature algorithms include: RSA, Elliptic Curve Digital Signature Algorithm (ECDSA), and Finite Automata-based digital signature algorithms, among others. Specialized digital signatures include group signatures, ring signatures, threshold signatures, blind signatures, proxy signatures, undeniable signatures, fair blind signatures, and signatures with message recovery capabilities.

2.2. Common digital signature

Group signatures, first introduced by Chaum and Van Heyst in 1991, allow group members to sign documents or messages using their group certificates and their private keys to generate a group signature.

As technology evolves, group signature schemes are also evolving to meet more complex scenario requirements. Backes[2] and others have studied the issue of member privacy protection in fully dynamic group signatures; Tang[3] and others have implemented a group signature method based on lattices with editable signatures and time-limited keys; Perera[3] and others have used a decentralized collaborative approach to analyze and study the tracking of group signers; Fu[4] and others have proposed a blockchain privacy protection technology monitoring scheme based on group signatures. Liu[5] and others have studied a decentralized system group signature method based on identity and optimization of the national secret SM2 algorithm.

Ring signatures were originally conceived and proposed in 2001 by Rivest, Adi Shamir, and Yael Tauman. They are a simplified version of group signatures. The signature generated has a certain parameter that forms a ring according to certain rules, hence the name ring signature. There is no need for a manager in ring signatures, nor is there a need for cooperation among ring members.

Currently, the industry's research on ring signatures is mainly focused on improving its security, efficiency, and practicality. Jingzhong[6] and others designed an electronic voting protocol based on ring signatures and secure multi-party computation; Kugusheva[7] and others implemented a blockchain voting method based on ring signatures; Yang[8] and others studied the design method of blockchain smart contracts based on ring signatures; Wang[9] and others studied a quantum ring signature scheme based on the quantum finite automaton signature method.

In 1991, Desmedt and Frankel made a groundbreaking proposal of the (t, n) threshold signature scheme, a milestone contribution that marked the digital signature method based on Multi-Party Computation (MPC) technology entering a new era. By splitting the private key and distributing it to multiple signers, a valid signature can only be generated when a certain number of signers participate.

The latest research progress in threshold signatures includes Tang[10] and others proposing an efficient threshold signature scheme based on lattices with functional interchangeability; Kachouh[11] and others have studied a threshold elliptic curve

digital signature algorithm for multi-party applications. In addition, with the continuous development and application of blockchain technology, threshold signature technology is expected to be more widely applied and promoted in the future.

The concept of blind signatures was first proposed by David Chaum in 1982. In blind signatures, the message holder submits an encrypted message, which has been blinded, to the signer for signing, making it a special type of digital signature method.

The latest research progress in blind signatures includes Shim[12] and others who analyzed the cryptography of lattice-based blind signatures and blind ring signature schemes; Ma[13] and others who designed an attribute-based blind signature scheme using elliptic curve cryptography; Jiang[14] and others who analyzed and constructed the cryptography in identity-based partial blind signature schemes; Sumathy[15] and others who designed a quantum blind signature protocol based on quantum teleportation and entanglement for quantum secure communication in security service bases.

In summary, the aforementioned widely used digital signature technologies have achieved significant results in terms of signer anonymity, untraceability of the signer, privacy protection of the message content, and signature security. However, the application demand for the signer to designate (authorize) a verifier, especially to designate (authorize) multiple verifiers within a group, still requires further research. In light of this, this study is committed to improving a method for authorized verification of signed messages between users in a multi-level group, in order to make up for the regret that existing digital signature technologies cannot authorize multiple verifiers within multi-level groups.

3. Research on Authorization Verification Methods for Message Signatures within Multi-Level Groups

3.1. Problem definition and formalization representation

The research scenario for the project is as follows: In a group G , there are n (where n is no less than 3) group members (users). A message signed by any user can only be verified and the original message retrieved by authorized group members; unauthorized group members are unable to obtain the original message. The core process is as follows:

Let: the group members be $U_i (i=1,2,..., n)$, the original message M , and the ciphertext C_i signed by U_i . Assuming that user U_i wants C_i to be received and decrypted only by users in U_{sup} , a subset of members in group G , the problem can be expressed as:

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$$\text{Sig}_{(U_i \rightarrow U_{sup})}(M) = C_i \quad (1)$$

$$\text{Ver}_{(U_j \in U_{sup})}(C_i) = M \quad (2)$$

In this context: Equation (1) indicates that a group member U_i signs the message M to produce a ciphertext C_i , and authorizes the members included in the subset U_{sup} to verify and decrypt it. Equation (2) states that a group member U_j , who is a part of

Experimental objectives:1) Verify correctness of encryption/decryption.;2) Evaluate stability as group size and authorised user count increase.Experimental results and analysis

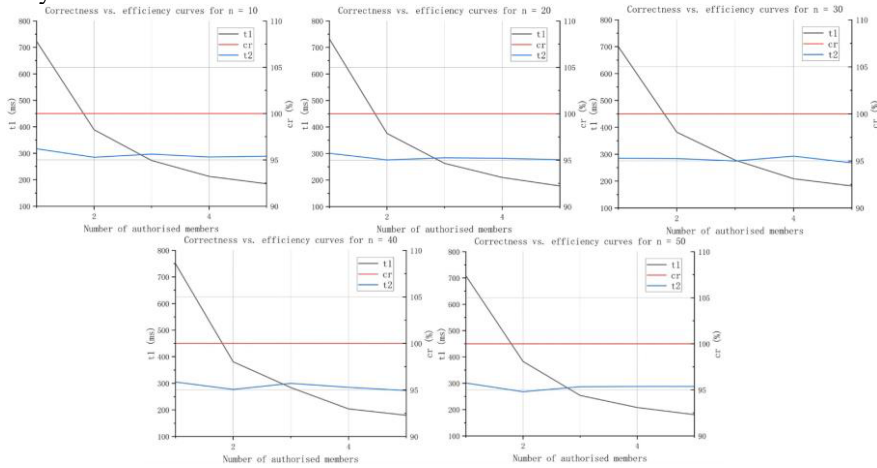


Figure 2.

Among Fig. 2. shows the correctness vs. efficiency curve for $n=10$, $n=20$, $n=30$, $n=40$, $n=50$. $cr(\%)$ is the algorithm correctness rate; $t1$ is the average encryption time; and $t2$ is the average decryption time of the authorised members.

Experimental data reveals that:(1) Regardless of group size, the accuracy (cr) of the core algorithm remains 100% as the number of authorized users increases.(2) Within each experiment, $t1$ fluctuations are within 500ms regardless of changes in b .(3) Encryption time is less correlated with group size n and more inversely related to the number of authorized users b .(4) $t2$ fluctuations are minor, unrelated to both n and b , consistent within and across experiments.

In conclusion, experiments and analysis confirm the reliability and stability of the proposed core algorithm, effectively accommodating authorization verification for multi-level, large-scale group message signatures.

5. Conclusions and Recommendations

In response to the reality that the demand for authorization verification in multi-level groups has not received enough attention, this paper proposes an algorithm that fuses message signatures to authenticate authorized verification users. The algorithm is implemented and experimentally verified, proving the reliability and stability of the proposed algorithm, specifically demonstrated by a 100% correct rate. Although the number of authorized verification users increases, the encryption time is independent of the number of group members and negatively correlated with the number of authorized users, with a fluctuation range of no more than 500ms. In terms of decryption time for authorized verification users, the fluctuation range is no more than 50ms and independent of the number of group members and authorized users. This indicates that the proposed algorithm is effective in adapting to the application of large-scale, multi-level group message signatures authorization verification, which is particularly valuable in hierarchical and role-based groups, such as government agencies,

enterprises, societies, etc. where group members need to be authorized to access different topics within the group.

It is evident from this study that the group size and the number of authorized users can be expanded to a wider range, such as $n=1000$ and $b=20$. In addition, the virtual machine technology used in this experiment can be ported to real distributed network nodes and further refined with possible network failures, low bandwidth, etc. to obtain more precise conclusions, which can guide related scene applications.

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