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# Geometrical Optimization of Axially Loaded Tubular Adhesive Joints by Finite Elements

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Abstract. Bonding with adhesives is increasingly being used in the design of mechanical structures. Tubular joints find applications in the piping industry, vehicle frames or thin-walled tubes, for instance, but they are seldom studied in the literature. This work numerically addressed the tensile strength of aluminum tubular joints, after validation of the numerical tool with experiments. The numerical analysis consisted of using the Finite Element (FE) method and cohesive zone models (CZM) to predict the joint strength. Numerically, the effect of the overlap length ( $L_0$ ) and the thickness of the inner and outer tubes ( $t_{SI}$  and  $t_{SE}$ , respectively) is addressed. The CZM technique was positively validated for the strength analysis of tubular joints. It was also shown that the joints' geometry and type of adhesive highly influence the joints' behaviour.

Keywords. Finite Elements; Cohesive Zone Models; Structural Adhesive; Tubular Joints; Geometric parameters.

# Introduction

Adhesive bonding is one of the most used joining methods nowadays and is widely studied due to its potential. As a result of improvements in the characteristics of adhesives, adhesive bonding has progressively replaced traditional joining methods such as bolting or riveting [1]. The aeronautical industry was the pioneer of this technology. The automotive and rail industries have also resorted to adhesives in order to obtain lighter structures. Other examples include construction, shoe making and electronics [2].

The strength prediction of bonded joints historically began with analytical stress analyses and then evolved to numerical methods. The finite element method has been used since the 70's and eventually turned out to be the most used technique for the adhesive joints analysis. In the review of He [3], FE methods applied to bonded joints are extensively discussed. More traditionally, FE-based strength prediction can rely on continuum or fracture mechanics approaches. Currently, the most widespread technique is CZM, which includes both stress and toughness properties to characterize the progressive failure process of bonded joints [4, 5]. CZM modeling depends on accurate

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values of cohesive strengths in tension and shear ( $t_n^0$  and  $t_s^0$ , respectively), and tensile ( $G_{IC}$ ) and shear toughness ( $G_{IIC}$ ) [6].

In the industry, several adhesive joint configurations can be used. The most commonly used are single-lap joints, as they are the easiest to conceive and load the adhesive mainly in shear. However, since the adherends are not collinear, a bending moment appears that creates peel efforts. To overcome this problem, joggle-lap, stepped-lap or double-lap joints can be used instead, since these allow a more uniform distribution of stresses, reducing the peeling efforts [1]. In addition, butt joints, T-joints, corner joints and tubular adhesive joints can be used in more specific applications. Tubular joints in particular have a large bonded area and a higher flexural strength due to their overall stiffness [1]. The use of adhesives for tube joining is one of the most recurrent methods today, and this technique presents an extensive application in the piping industry. A few studies are available that deal with the analysis of tubular joints. Dragoni and Goglio [7] studied the accuracy of five theoretical models for the prediction of adhesive layer stresses produced by axial loads in tubular adhesive joints, and compared the results with the FEM. It was concluded that, within all models considered, only that of Lubkin and Reissner [8] gives a truthful distribution of the peel stress in the overlap.

This work numerically addressed the tensile strength of aluminum tubular joints, after validation of the numerical tool with experiments. The numerical analysis consisted of using the FE method and CZM to predict the joint strength. Numerically, the geometrical optimization addresses the effect of  $L_0$  and the thickness of the inner and outer tubes ( $t_{SI}$  and  $t_{SE}$ , respectively).

## 1. Experimental work

## 1.1. Materials

Tubular joints between AW6082 T651 aluminium alloy adherends were considered. The characterization of this alloy in bulk tension, following the standard ASTM-E8M-04, is detailed in [9]. The following mechanical properties were attained: Young's modulus (*E*) of 70.07±0.83 GPa, tensile yield stress ( $\sigma_y$ ) of 261.67±7.65 MPa, tensile failure strength ( $\sigma_f$ ) of 324±0.16 MPa and tensile failure strain ( $\varepsilon_f$ ) of 21.70±4.24%.

Property	
Young's modulus, E [GPa]	1.85±0.21
Poisson's ratio, v	0.33 <sup>a</sup>
Tensile yield stress, $\sigma_y$ [MPa]	$12.63 \pm 0.61$
Tensile strength, $\sigma_{\rm f}$ [MPa]	$21.63 \pm 1.61$
Tensile failure strain, $\varepsilon_{\rm f}$ [%]	4.77±0.15
Shear modulus, G [GPa]	$0.56 \pm 0.21$
Shear yield stress, $\tau_y$ [MPa]	$14.6 \pm 1.3$
Shear strength, $\tau_{\rm f}$ [MPa]	$17.9 \pm 1.8$
Shear failure strain, $\gamma_f$ [%]	43.9±3.4
Toughness in tension, G <sub>IC</sub> [N/mm]	$0.43{\pm}0.02$
Toughness in shear, G <sub>IIC</sub> [N/mm]	$4.70 \pm 0.34$

Table 1. Mechanical and fracture properties of the adhesive Araldite® 2015 [10, 11].

<sup>a</sup> manufacturer's data

The ductile epoxy adhesive Araldite<sup>®</sup> 2015 was considered to fabricate the tubular joints. Mechanical and fracture characterization of this adhesive was properly undertaken in a previous works [10, 11]. The tensile mechanical properties were defined by tensile tests to bulk specimens, which enabled the estimation of E,  $\sigma_y$ ,  $\sigma_f$  and  $\varepsilon_f$ . On the other hand, the Thick Adherend Shear Tests (TAST) was used for estimation of the shear mechanical properties, with C45E steel adherends. The relevant fracture properties of the adhesives ( $G_{IC}$  and  $G_{IIC}$ ) were obtained from Double-Cantilever Beam (DCB) and End-Notched Flexure (ENF) tests, respectively [11, 12]. The adhesive's properties used in the simulations are described in Table 1.

#### 1.2. Experimental details

Figure 1 represents the geometry of the tubular joints and the associated geometric parameters (dimensions in mm):  $L_0=20$  and 40, adherends' free length  $L_S=50$  for  $L_0=20$  and 60 for  $L_0=40$ , joint free length  $L_T=80$ , outer diameter if the inner tube  $d_{SE}=22.4$ ,  $t_{SE}=2$  and adhesive thickness  $t_A=0.2$ .



Figure 1. Geometry and characteristic dimensions of the tubular joints.

Testing of the specimens was carried out in a Shimadzu-Autograph AG-X tester, equipped with a 100 kN load cell, at room temperature and with a velocity of 1 mm/min. The tests resulted in individualized load-displacement (P- $\delta$ ) curves that will enable comparison with the numerical results.

# 2. Numerical work

#### 2.1. Simulation settings

The Abaqus<sup>®</sup> software was chosen to perform the CZM analysis of the tubular joints. The aluminium tubes were modelled using solid elasto-plastic elements, as per the  $\sigma$ - $\varepsilon$  curves of reference [13]. CZM elements with a triangular mixed-mode law (further defined in this work) were used for the adhesive. Due to the particular characteristics of the tubular joints' geometry, i.e., with axisymmetric geometry, loads and boundary conditions, a two-dimensional (2D) axisymmetric FE study was considered. Figure 2 shows the mesh refinement for the tubular joint model with  $L_0=20$  mm. In which concerns the applied boundary conditions, the tubes were clamped at one of the edges and pulled longitudinally while transversely restrained at the opposite edge.

Figure 2. FE mesh detail of the axisymmetric model for a tubular with  $L_0=20$  mm.

# 2.2. Traingular CZM model

CZM laws simulate the elastic behaviour up to a peak load and subsequent softening, to model the gradual degradation of material properties up to complete failure. The areas under the traction-separation laws in tension or shear are equalled to  $G_{\rm IC}$  or  $G_{\rm IIC}$ , respectively. Under pure mode, damage propagation occurs at a specific integration point when the stresses are released in the respective traction-separation law. Under mixed mode, energetic criteria are often used to combine tension and shear [14]. In this work, triangular pure and mixed-mode laws, i.e. with linear softening, were considered. In this work, the quadratic nominal stress criterion was considered for the initiation of damage. Complete separation is predicted by a linear power law form of the required energies for failure in the pure modes. For full details of the presented model, see reference [10].

# 3. Results

# 3.1. Validation with experimental results

In this Section, the results from the experimental tests are presented, followed by the comparison with the CZM strength predictions, for evaluation of this technique.

## 3.1.1. Experimental results

Figure 3 summarizes the maximum load ( $P_m$ ) obtained as a function of  $L_0$ . The joints have  $P_m \approx 27.2$  kN for  $L_0=20$  mm. A large  $P_m$  increase with  $L_0$  was also found because this adhesive has moderate ductility and, therefore, higher loads can be reached by the effect of adhesive plasticization. The percentile increase between the two tested  $L_0$  is 43.4%, corresponding to  $P_m \approx 39.1$  kN for  $L_0=40$  mm. Under these conditions, plasticization of the inner tube was also detected after the tests.



Figure 3. Experimental  $P_{\rm m}$  as a function of  $L_{\rm O}$  for the tubular joints.

#### 3.1.2. Strength prediction by CZM

This study aims to check the validity of CZM in predicting the behaviour of the tubular joints, by the comparison between numerical and average experimental values of  $P_{\rm m}$ . Figure 4 provides this comparison as a function of  $L_{\rm O}$ . The results generally show that the CZM and experimental  $P_{\rm m}$  values are very close for the tubular joints. The percentile difference between the experimental and numerical  $P_{\rm m}$  is 6.1% for  $L_{\rm O}$ =20 mm. This deviation becomes even lower for  $L_{\rm O}$ =40 mm (2.9%). These results clearly show that the triangular CZM model is also accurate. Therefore, the numerical  $P_{\rm m}$  values are accepted, despite the respective dispersion of values.



Figure 4. Evaluation of the predicted  $P_m$  against the experimental results for the tubular joints.

# 3.2. Effect of the geometric parameters

 $L_{\rm O}$  and the adherends' thickness were considered.  $L_{\rm O}$  was varied between 10 mm and 50 mm. The parametric analysis considered: (1) change of  $t_{\rm SI}$ ; (2) variation of  $t_{\rm SE}$  and (3) variation of both  $t_{\rm SI}$  and  $t_{\rm SE}$ .  $L_{\rm O}$ =40 mm was used for all analyses. Moreover, for the studies in which either  $t_{\rm SI}$  or  $t_{\rm SE}$  is kept constant, its value was fixed at 2 mm.

#### 3.2.1. Overlap length

The variation of  $L_0$  is initially addressed numerically. Figure 5 shows the P- $\delta$  curves obtained by the CZM numerical analysis as a function of  $L_0$ . From the evaluation of these curves it is possible to assess  $P_m$  and acknowledge its evolution with  $L_0$ . The tubular joints showed a linear behavior up to  $L_0=20$  mm.

From  $L_0=30$  mm, the inner aluminum tubes begin to develop massive plastic strains accompanied with their necking (Figure 6), due to the ductility of this adhesive and high loads achieved. This behavior is detected in the *P*- $\delta$  curves for  $L_0=30$  mm (reduced necking before failure in the adhesive layer) and  $L_0=40$  and 50 mm (extensive necking).



Figure 5. Numerical P- $\delta$  curves for the tubular joints as a function of  $L_0$ .



Figure 6. Necking in the inner tube of the tubular joint with  $L_0=40$  mm.

Figure 7 depicts the evolution of  $P_{\rm m}$  with  $L_{\rm O}$  for the tubular joints. The  $P_{\rm m}$  increase between  $L_0=10$  and 20 mm was practically linear (increase of 98.7%), in view of the ductility of the Araldite® 2015, which manages to fail under global yielding conditions for these small  $L_0$ . For bigger  $L_0$ , failure occurred by necking of the inner tube and, thus, a stabilization of  $P_m$  was found. As a result, for the set of geometrical and material conditions tested in this work, there is no advantage in the design with  $L_0>30$  mm.



Figure 7. Numerical  $P_{\rm m}$  as a function of  $L_{\rm O}$  for the tubular joints.

#### 3.2.2. Adherends' thickness

As previously described, the adherends' thickness analysis comprises the variation of  $t_{SI}$ ,  $t_{SE}$  and  $t_{SI}$  plus  $t_{SE}$ . Figure 8 shows the numerical *P*- $\delta$  curves for the tubular joints as a function of  $t_{SI}$  (a),  $t_{SE}$  (b) and  $t_{SI}$  plus  $t_{SE}$  (c), obtained by the CZM analysis.



**Figure 8**. Numerical *P*- $\delta$  curves for the tubular joints as a function of  $t_{SI}$  (a),  $t_{SE}$  (b) and  $t_{SI}$  plus  $t_{SE}$  (c).

The *P*- $\delta$  curves relating to the  $t_{SI}$  effect show a gradual increase of  $P_m$  as  $t_{SI}$  increases, but a stabilization of  $P_m$  for  $L_O \ge 30$  mm. Nonetheless, all *P*- $\delta$  curves point out to necking of the adherends. The tendency was much different for the variation of  $t_{SE}$ . Actually, for  $t_{SE}=1$  mm, the tubular joint failed by necking of the outer adherend due to its reduced cross-sectional area, and revealed a major  $P_m$  difference to the other  $t_{SE}$ . For higher  $t_{SE}$ , the behavior was always identical, and failure took place by necking of the inner tube. Finally, for the variation of  $t_{SI}$  plus  $t_{SE}$ , all failures up to  $t_{SI}=t_{SE}=2$  mm occurred by necking of the inner adherend. The joint with  $t_{SI}=t_{SE}=1$  mm showed the worst results, due to the naturally longitudinal tensile strength of the inner tube, which reflected on necking occurrence for smaller applied loads to the joint.  $P_m$  increased steadily up to  $t_{SI}=t_{SE}=3$  mm but, above this value (inclusively), failure no longer took place in the adherends due to its increased cross-section, but instead by cohesive failure of the adhesive layer. Thus,  $P_m$  is identical for  $t_{SI}=t_{SE}\ge 3$  mm.



**Figure 9.** Numerical  $P_{\rm m}$  as a function of  $t_{\rm SI}$  (a),  $t_{\rm SE}$  (b) and  $t_{\rm SI}$  plus  $t_{\rm SE}$  (c) for the tubular joints.

Figure 9 depicts the summary of the numerical  $P_m$  as a function of  $t_{SI}$  (a),  $t_{SE}$  (b) and  $t_{SI}$  plus  $t_{SE}$  (c) for the tubular joints. In accordance with the previous P- $\delta$  curves' analysis, for the variation of  $t_{SI}$ , no advantage exits in  $t_{SI}$ >3 mm, since necking of the outer tube always exists. However, compared to the initial geometry ( $t_{SI}$ = $t_{SE}$ =2 mm), a 24.6% strength improvement. The increase of  $t_{SE}$  ceased to reflect on  $P_m$  for  $t_{SE} \ge 2$  mm because the traditionally weaker element, the inner tube, is left unchanged. For concurrent variations of  $t_{SI}$  and  $t_{SE}$ , the inner tube's necking was responsible for joint failure up to  $t_{SI}$ = $t_{SE}$ =2 mm. For bigger values of these parameters, cohesive failures of the adhesive were found. Thus, the optimal geometry with identical diameter tubes is  $t_{SI}$ = $t_{SE}$ =3 mm.

# 4. Conclusions

The proposed work addressed the tensile strength of aluminum tubular joints, after validation of the numerical tool with experiments. The experimental tests revealed a large  $P_{\rm m}$  increase with  $L_0$  because of the ductility of the Araldite<sup>®</sup> 2015. The percentile increase between the two tested  $L_0$  was 43.4%. For  $L_0$ =40 mm, plasticization of the inner tube was detected after the tests. The validation results showed that the CZM and experimental  $P_{\rm m}$  values were very close for the tubular joints. Thus, it was considered that the CZM analysis is suitable to perform the parametric study was undertaken next in the paper. The variation of  $L_0$  had a significant influence on  $P_{\rm m}$ . The  $P_{\rm m}$  increase between  $L_0$ =10 and 20 mm was practically linear (increase of 98.7%). However, for bigger  $L_0$ , failure occurred by necking of the inner tube and, thus, a stabilization of  $P_{\rm m}$  was found. Regarding the tubes' thickness effect, for the variation of  $t_{\rm SI}$ , no advantage

exits in  $t_{SI}>3$  mm, since necking of the outer tube always exists. The increase of  $t_{SE}$  ceased to reflect on  $P_m$  for  $t_{SE}\ge2$  mm because the traditionally weaker element, the inner tube, is left unchanged. For concurrent variations of  $t_{SI}$  and  $t_{SE}$ , the inner tube's necking was responsible for joint failure up to  $t_{SI}=t_{SE}=2$  mm. For bigger values of these parameters, cohesive failures of the adhesive were found. Thus, the optimal geometry with identical diameter tubes is  $t_{SI}=t_{SE}=3$  mm.

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